# Marcinkiewicz-Zygmund type law of large numbers for double arrays of random elements in Banach spaces

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Abstract: In this paper we establish Marcinkiewicz-Zygmund type laws of large numbers for double arrays of random elements in Banach spaces. Our results extend those of Hong and Volodin [6]. © Pleiades Publishing, Ltd., 2009.

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