# Operational properties of two integral transforms of fourier type and their convolutions

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Abstract: In this paper we present the operational properties of two integral transforms of Fourier type, provide the formulation of convolutions, and obtain eight new convolutions for those transforms. Moreover, we consider applications such as the construction of normed ring structures on L1(), further applications to linear partial differential equations and an integral equation with a mixed Toeplitz-Hankel kernel. © 2009 Birkhäuser Verlag Basel/Switzerland.
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