Optimal adaptive sampling recovery

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Abstract: We propose an approach to study optimal methods of adaptive sampling recovery of functions by sets of a finite capacity which is measured by their cardinality or pseudo-dimension. Let W L_q, $0 < q \leq \infty$, be a class of functions on {Mathematical expression}. For B a subset in L_q, we define a sampling recovery method with the free choice of sample points and recovering functions from B as follows. For each f W we choose n sample points. This choice defines n sampled values. Based on these sampled values, we choose a function from B for recovering f. The choice of n sample points and a recovering function from B for each f W defines a sampling recovery method {Mathematical expression} by functions in B. An efficient sampling recovery method should be adaptive to f. Given a family {Mathematical expression} of subsets in L_q, we consider optimal methods of adaptive sampling recovery of functions in W by B from {Mathematical expression} in terms of the quantity {Mathematical expression}Denote {Mathematical expression} by $e_n(W)_q$ if {Mathematical expression} is the family of all subsets B of L_q such that the cardinality of B does not exceed 2^n, and by $r_n(W)_q$ if {Mathematical expression} is the family of all subsets B in L_q of pseudo-dimension at most n. Let $0 < p, q, \theta \leq \infty$ and α satisfy one of the following conditions: (i) $\alpha > d/p$; (ii) $\alpha = d/p$, $\theta \leq \min(1, q)$, $p, q < \infty$. Then for the d-variable Besov class {Mathematical expression} (defined as the unit ball of the Besov space {Mathematical expression}), there is the following asymptotic order {Mathematical expression}To construct asymptotically optimal adaptive sampling recovery methods for {Mathematical expression} and {Mathematical expression} we use a quasi-interpolant wavelet representation of functions in Besov spaces associated with some equivalent discrete quasi-norm. © 2009 Springer Science+Business Media, LLC.

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