

# Recursive properties of Dirac and metriplectic Dirac brackets with applications

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**Abstract:** In this article, we prove that Dirac brackets for Hamiltonian and non-Hamiltonian constrained systems can be derived recursively. We then study the applicability of that formulation in analysis of some interesting physical models. Particular attention is paid to the feasibility of implementation code for Dirac brackets in Computer Algebra System. © 2008 Elsevier B.V. All rights reserved.

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