

# On A-generators for the cohomology of the symmetric and the alternating groups

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**Abstract:** Following Quillen's programme, one can read off a lot of information on the cohomology of a finite group  $G$  by studying the restriction homomorphism from this cohomology to the cohomology of all maximal elementary abelian subgroups of  $G$ . This leads to a natural question on how much information on A-generators of  $H^*(G)$  one can read off from using the restriction homomorphism, where  $A$  denotes the Steenrod algebra. In this paper, we show that the restriction homomorphism gives, in some sense, very little information on A-generators of  $H^*(G)$  at least in the important three cases, where  $G$  is either the symmetric group, the alternating group, or a certain type of iterated wreath products. © 2005 Cambridge Philosophical Society.

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